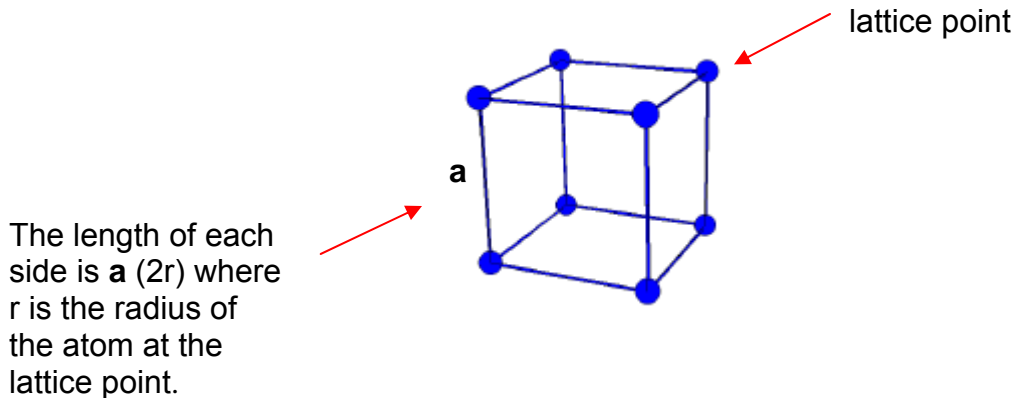


## Simple Cubic Lattice

Crystalline solids are those solids, unlike amorphous solids, that have a regular and repeating arrangement of atoms. Each of these crystalline solids consists of a unit cell which is a small group of atoms that contain unique features. When a large number of these unit cells are stacked together, they form a macroscopic crystal. The three cubic crystal types are the simple cubic lattice (primitive cubic), body-centered cubic, and the face-centered cubic. The simple cubic unit cell is shown below.



The length of a side of the unit cell,  $a$ , is called the lattice constant. An important feature of a crystal structure is the nearest distance between atomic centers (nearest-neighbor distance) and for the primitive cubic this distance is  $a$ .

A simple cubic lattice has eight lattice points where a lattice point is defined as a point of intersection of two or more grid lines. Each lattice point, eight in the diagram above, is a “site” for an atom to reside. **However, the unit cell above does not contain 8 atoms but only 1.** When considering cubic lattices, one must always think in terms of 3-D. Atoms at the corners of any cube are shared by 8 contiguous units cells, so only  $1/8$  of an atom is attributed to a single lattice point. Therefore,

$$1/8 \text{ atom/lattice point} \times 8 \text{ lattice points} = 1 \text{ atom}$$

An interesting property of primitive cubic cells is that of packing efficiency where

$$PE = V_a/V_{uc} \times 100\%$$

and  $V_a$  is the volume of the atoms occupying the interior of the cell and  $V_{uc}$  is the volume of the unit cell.

$V_a = 4/3 \cdot \pi \cdot r^3 \cdot Z$  where  $r$  is the atomic radius and  $Z$  the number of atoms contained within the unit cell.

$$V_r = l \cdot w \cdot h = w \cdot w \cdot w = (2r)^3 = 8r^3$$

$$PE = 4/3 \cdot \pi \cdot r^3 \cdot Z / 8r^3 \times 100\% = 52\% \text{ which applies to all primitive cubic cells.}$$

The graphic used in this tutorial was taken from the Crystal Lattice Structures Web page, <http://cst-www.nrl.navy.mil/lattice/> provided by the Center for Computational Materials Science of the United States Naval Research Laboratory.